

Earth gravity field recovery using GPS, GLONASS, and SLR satellites

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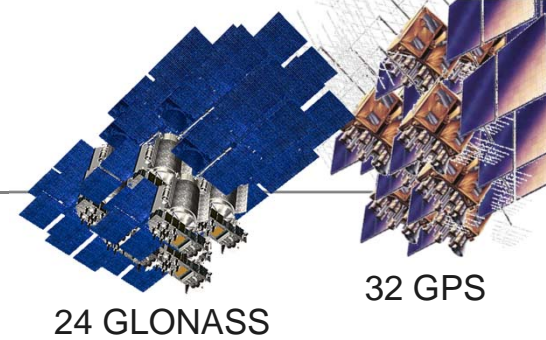
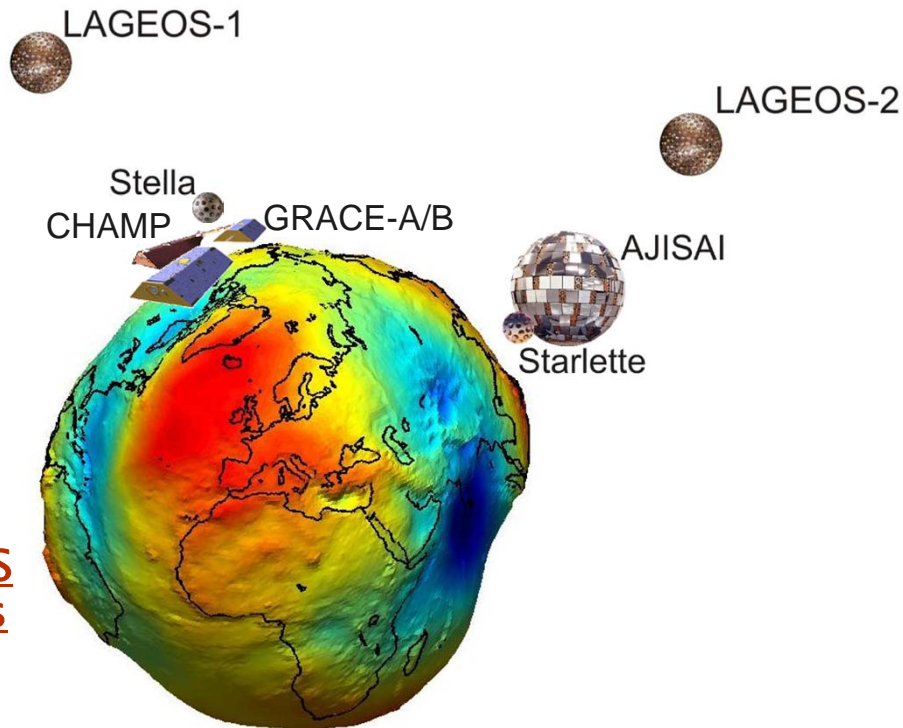
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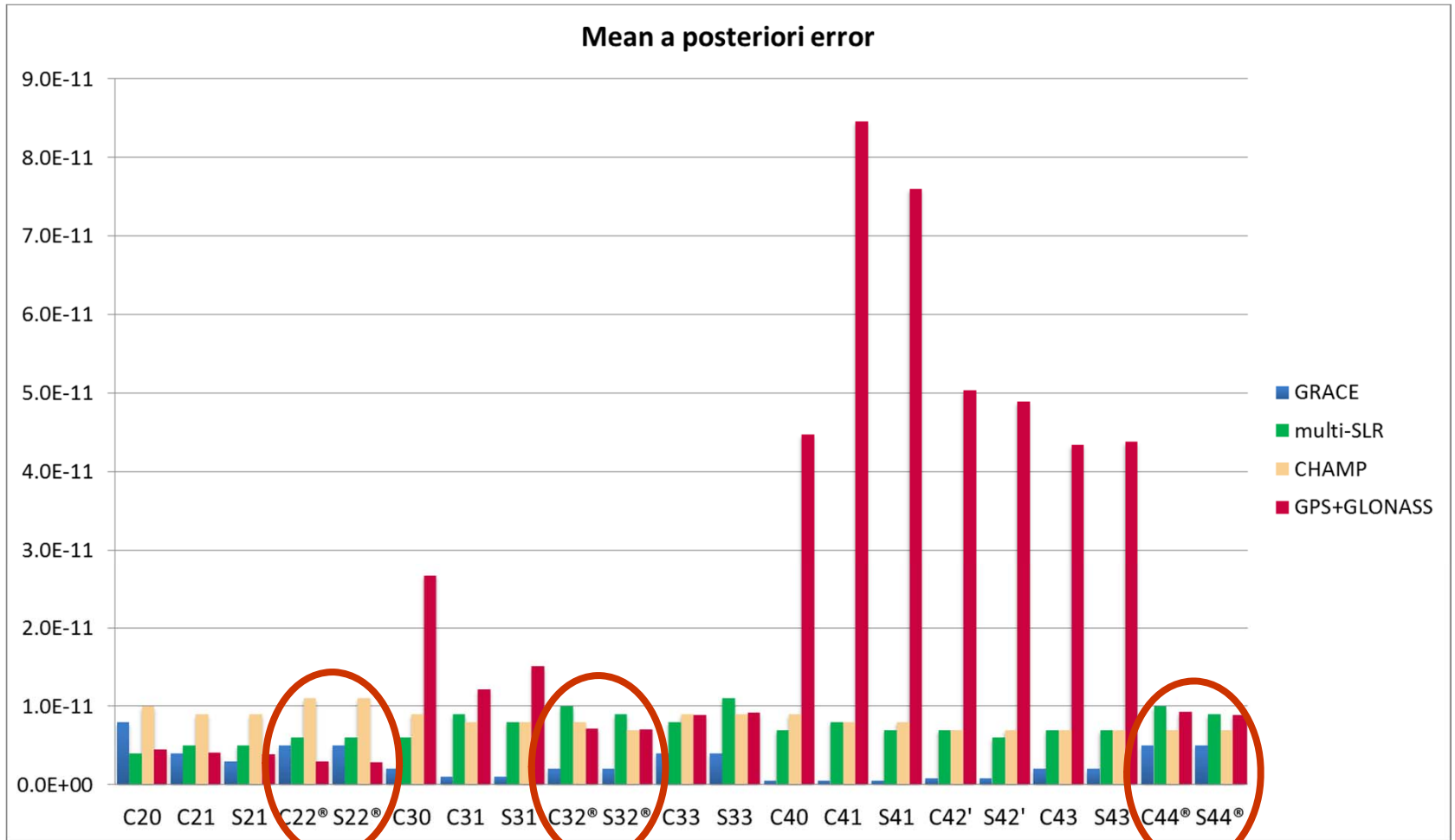
Motivation

Time-variable Earth's gravity field can be determined from:

- K-Band GRACE observations,
- GPS-derived positions of LEO satellites (e.g., CHAMP),
- Orbit perturbations:
 - using SLR to geodetic satellites,
 - using GPS and GLONASS microwave observations



Sensitivity of GPS resonant orbits



GNSS satellites are very sensitive to gravity field coefficients of degree 2. For coefficients above degree 3, GNSS are only sensitive to **resonant gravity field parameters** (®).

Solution set-up

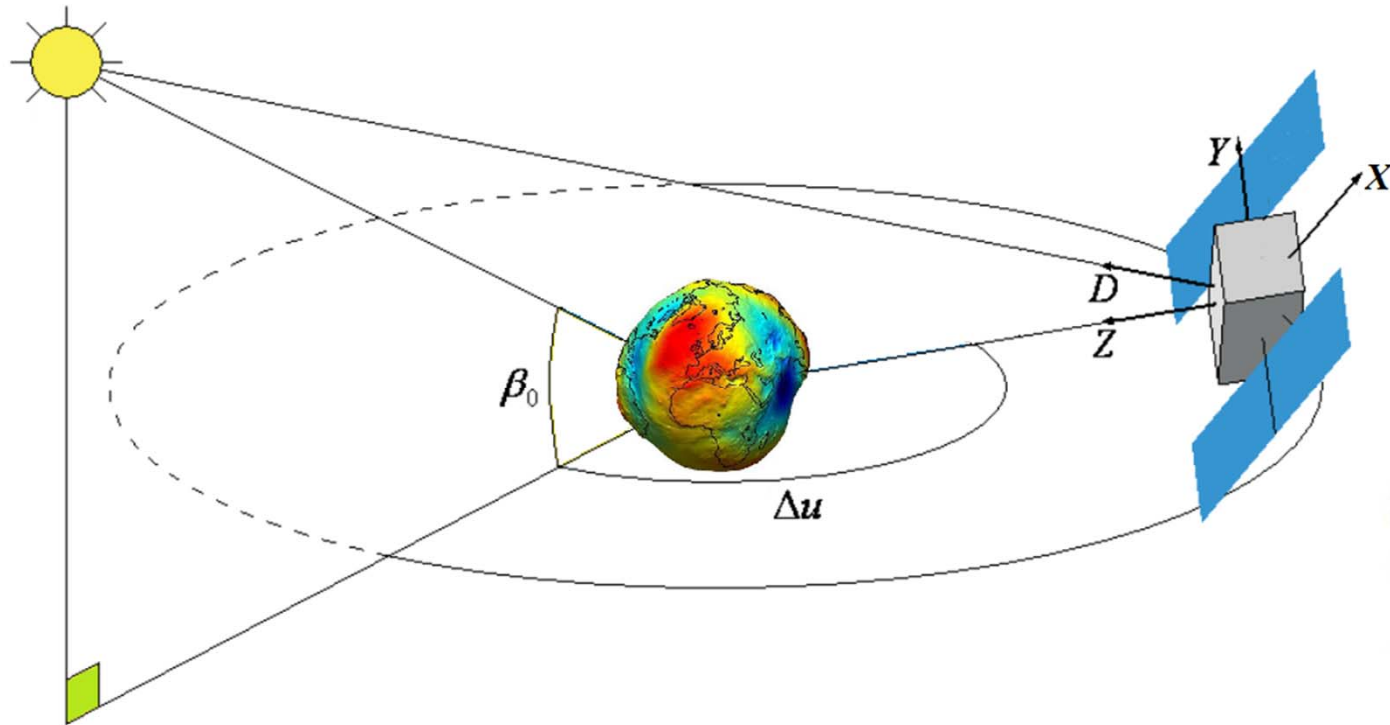
Estimated parameters		GNSS solutions	SLR solutions
		up to 32 GPS and 24 GLONASS satellites	LAGEOS-1/2, Starlette, Stella, Ajisai
Orbits	Osculating elements	a, e, i, Ω , ω , u_0 (1 set per 3 days)	a, e, i, Ω , ω , u_0 (1 set per 7 days)
	Dynamical parameters	D_0 , Y_0 , X_0 , X_S , X_C (1 set per 3 days)	LAGEOS-1/2: S_0 , S_C , S_S (1 set per 7 days) Sta/Ste/Aji: C_D , S_C , S_S , W_C , W_S (1 set per day)
	Pseudo-stochastic pulses	R, S, W (once per revolution)	LAGEOS-1/2: no pulses Sta/Ste/Aji: S (once per revolution)
Earth rotation parameters		X_p , Y_p , UT1-UTC (1 set per day)	X_p , Y_p , UT1-UTC (1 set per day)
Geocenter coordinates		1 set per 7 days	1 set per 7 days
Earth gravity field		Estimated up to d/o 4/4 (1 set per 7 days)	Estimated up to d/o 4/4 (1 set per 7 days)
Station coordinates		1 set per 7 days	1 set per 7 days
Other parameters		Troposphere ZD (2h), gradients (24h), GNSS-specific translations and ZTD biases	Range biases for selected stations

GNSS solutions are similar to the standard IGS solutions provided by CODE (Center for Orbit Determination in Europe), with some exceptions: **Earth gravity field parameters** are simultaneously **estimated** and 7-day instead of 1-day solutions are generated.

SLR solutions are similar to the standard ILRS solutions provided by BKG, **but more satellites** are included (Sta/Ste/Aji) and Earth **gravity field parameters** are **estimated**.

GPS+GLONASS solutions

GNSS orbit modeling



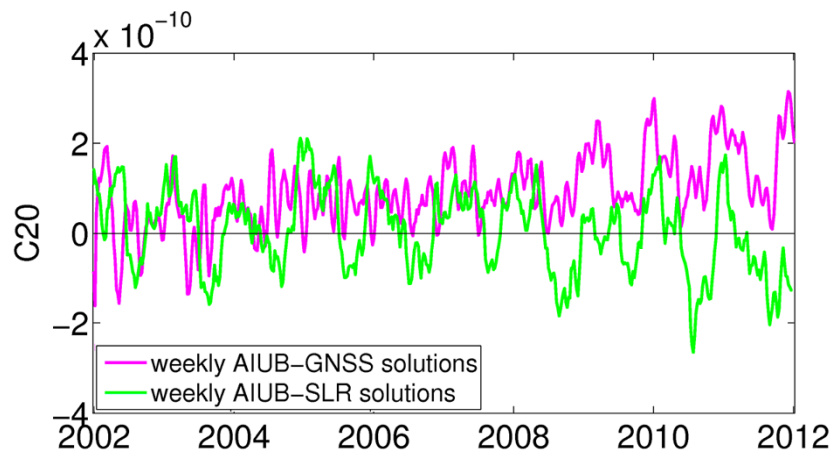
GNSS dynamic orbit parameters estimated in standard CODE solutions:

$$D = D_0$$

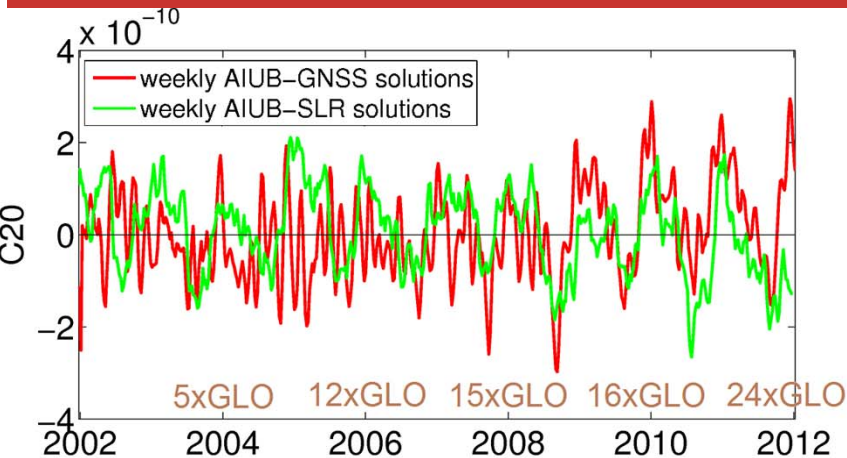
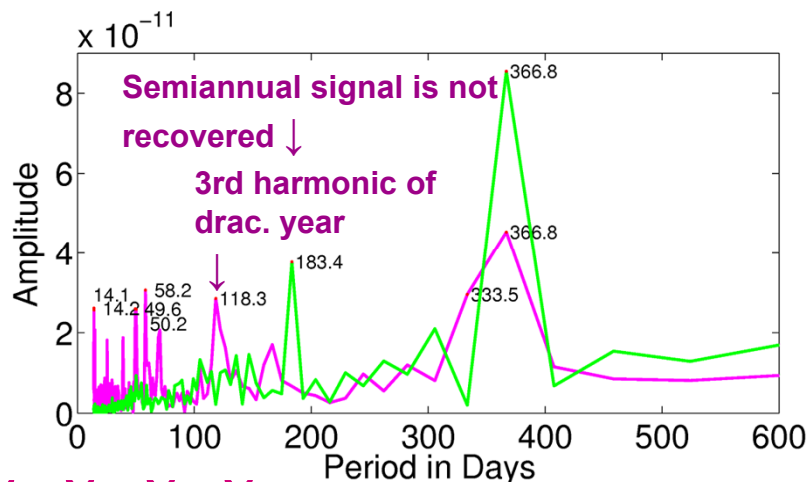
$$Y = Y_0$$

$$X = X_0 + X_s \sin \Delta u + X_c \cos \Delta u$$

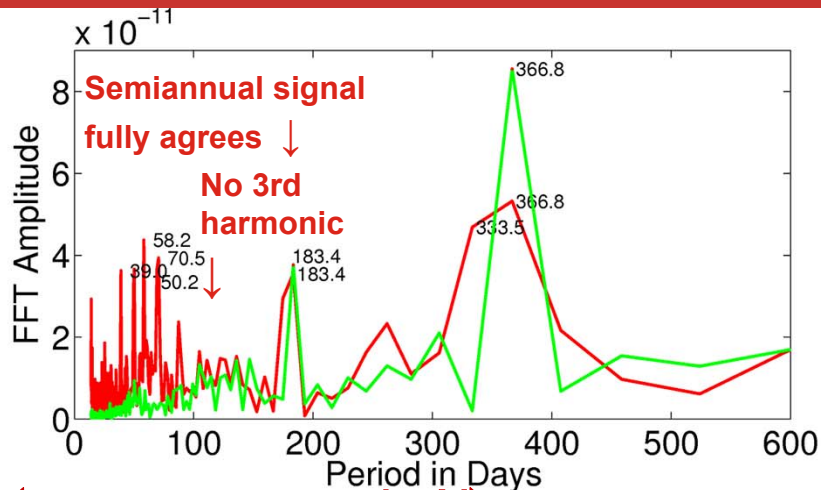
C₂₀ from GPS and GLONASS



GNSS dynamic orbit parameters :D₀, Y₀, X₀, X_s, X_c



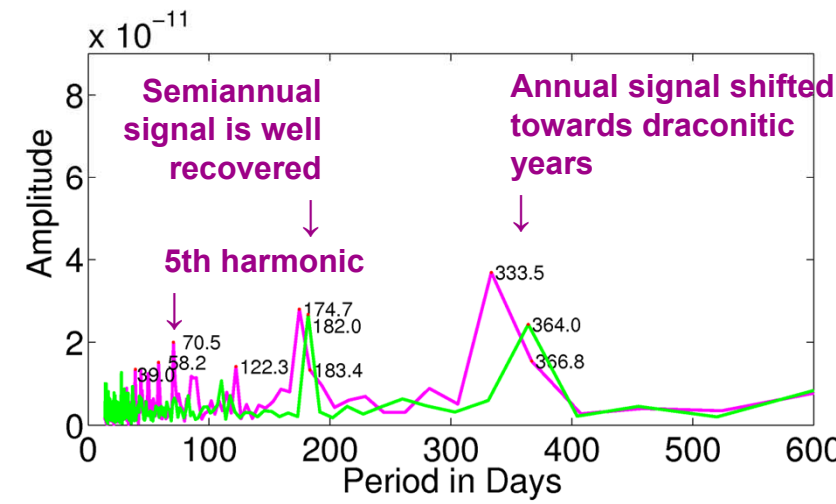
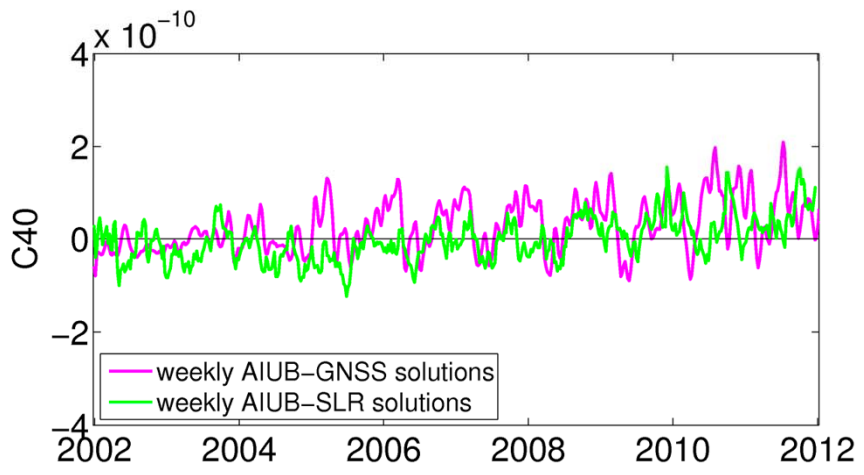
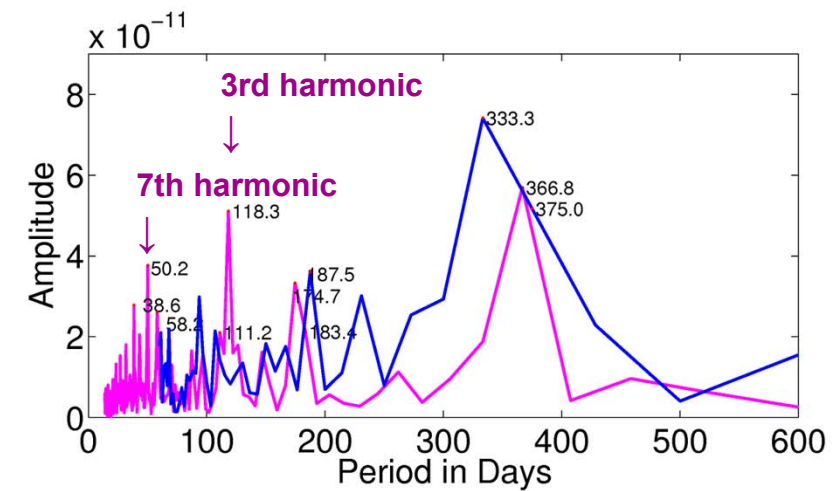
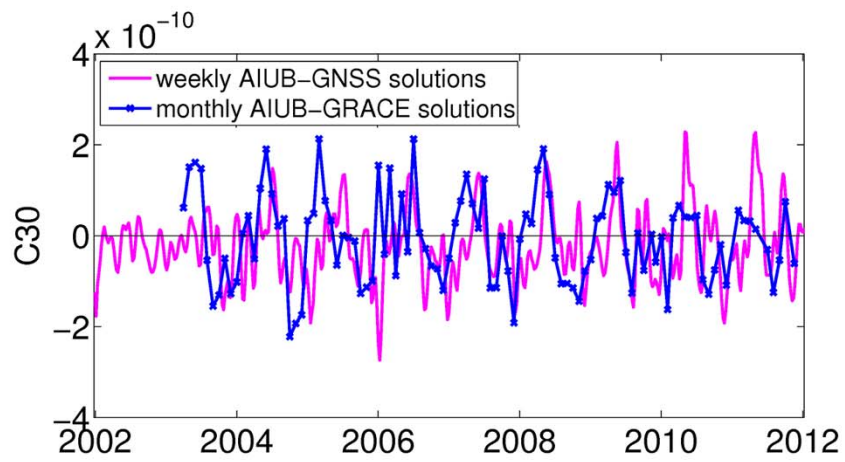
GNSS dynamic orbit parameters :D₀, Y₀ (no parameters in X)



These issues need further investigations

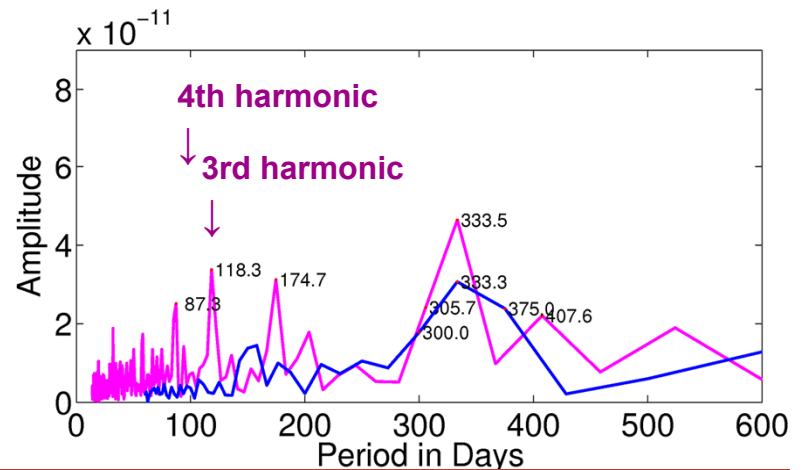
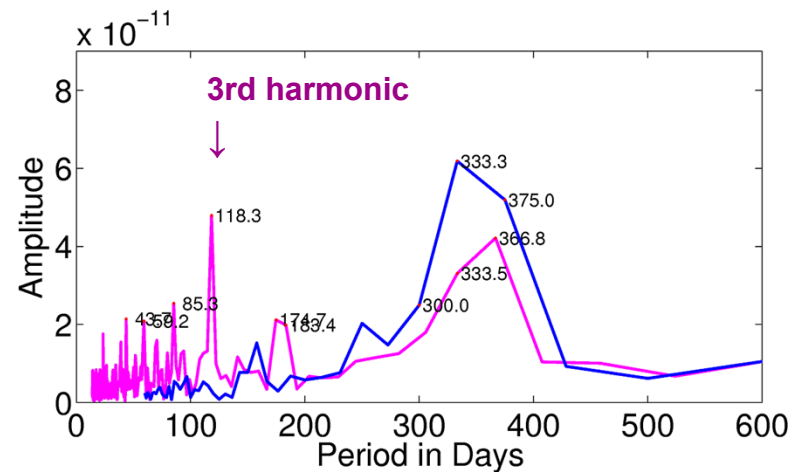
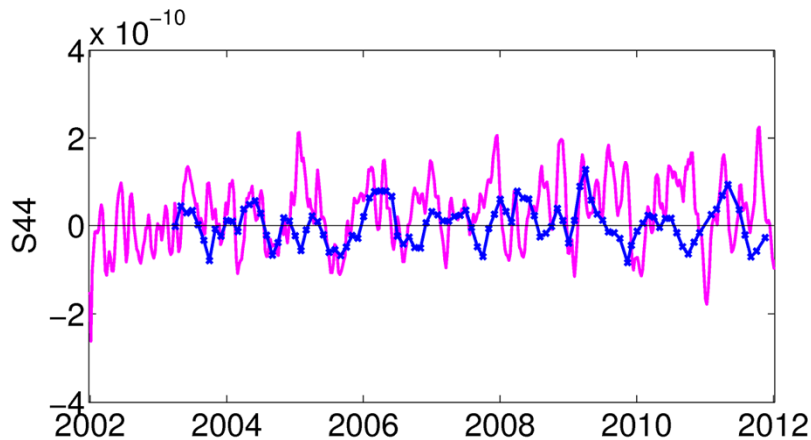
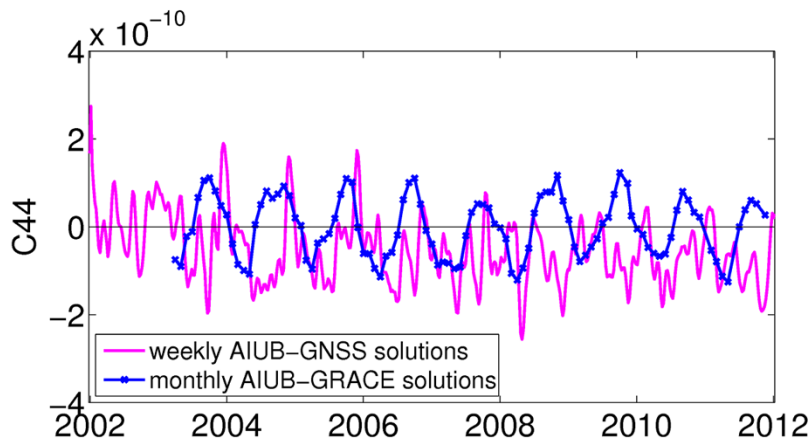
Zonal spherical harmonics from GPS and GLONASS

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Zonal harmonics can be recovered by GNSS to some extent

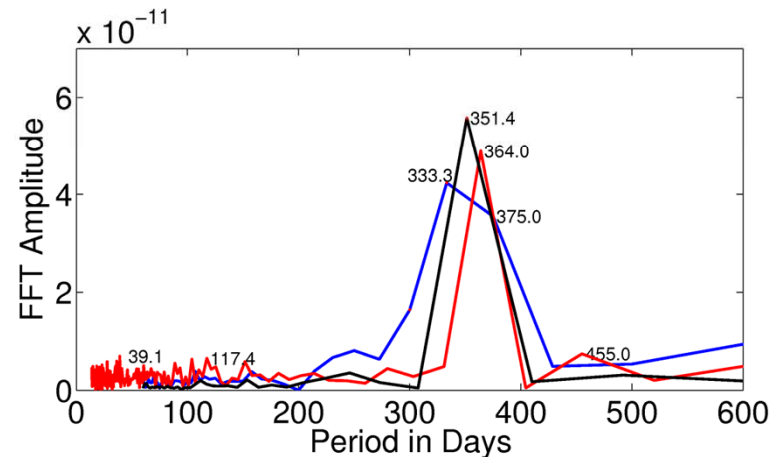
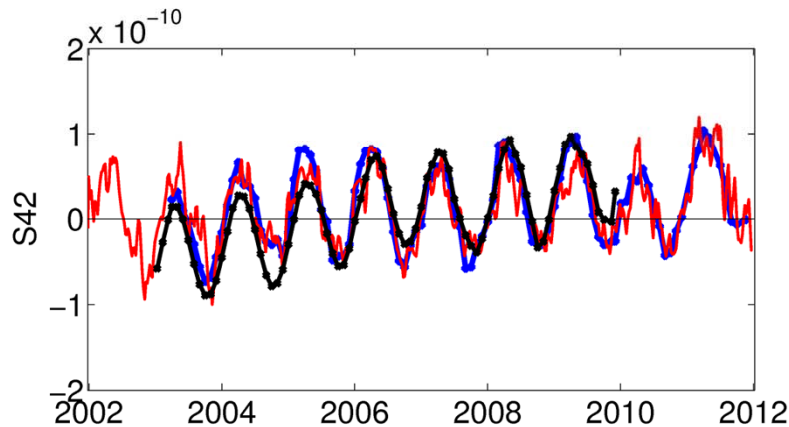
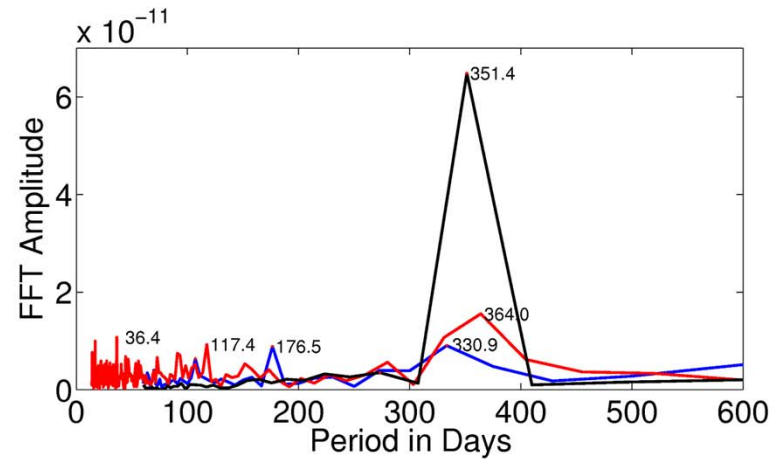
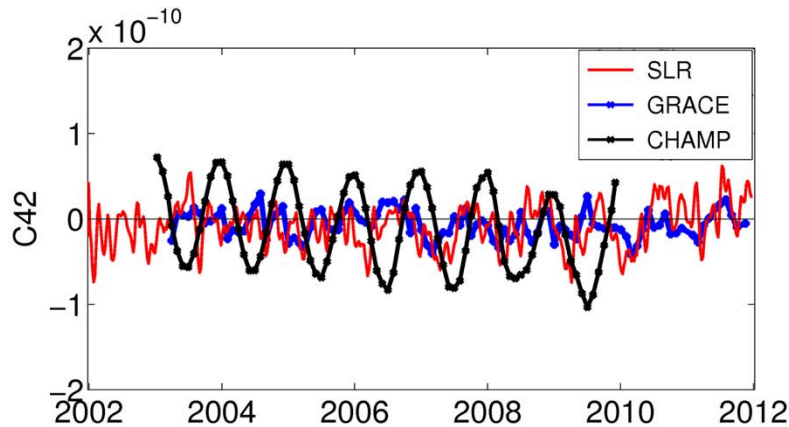
Resonant GPS harmonics



Resonant harmonics, despite a large sensitivity, cannot be fully recovered by GNSS, because of the correlations with D_0 .

SLR solutions

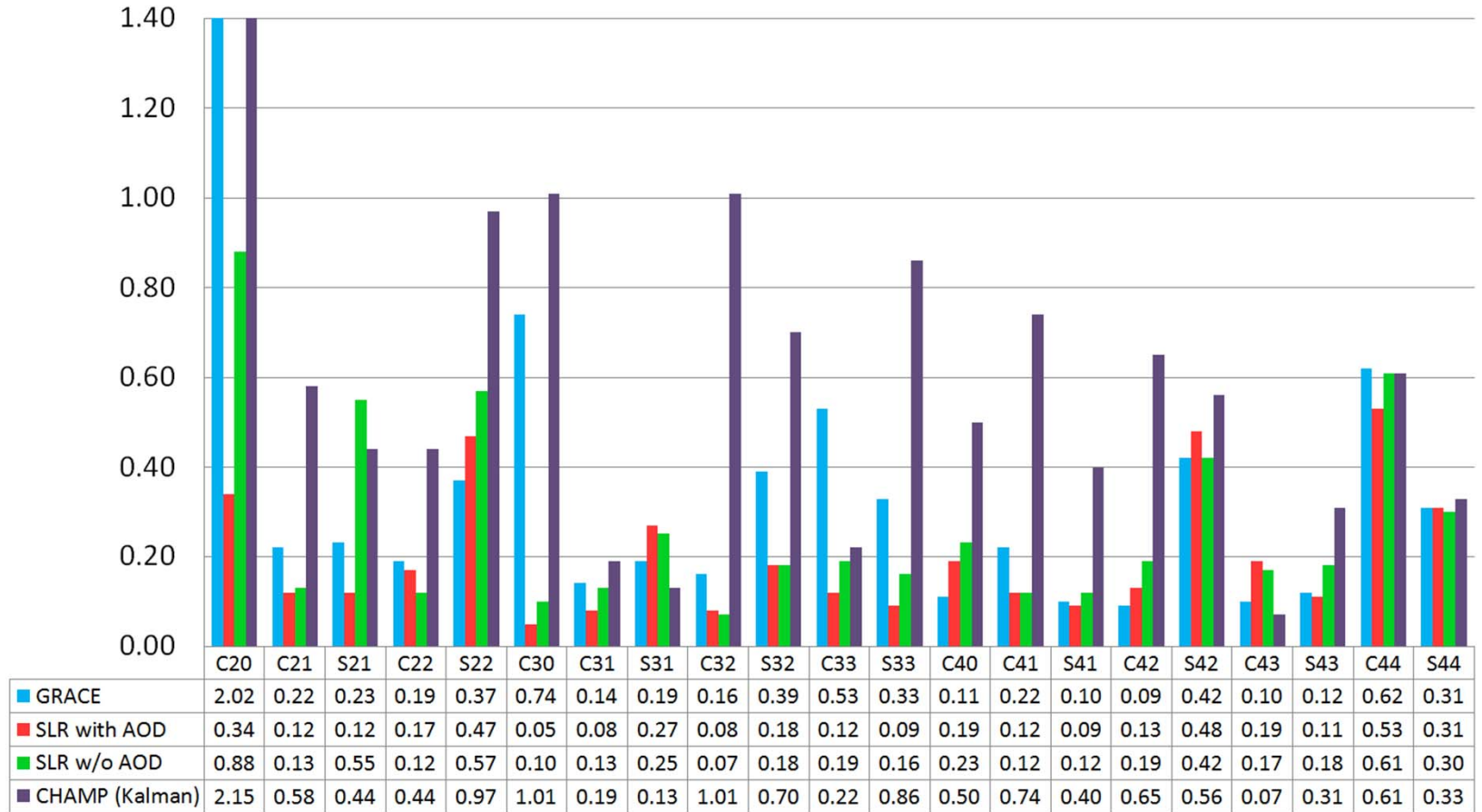
SLR vs. CHAMP vs. GRACE



Some coefficients derived by SLR, CHAMP, and GRACE solutions agree very well. CHAMP solutions show typically larger amplitudes.

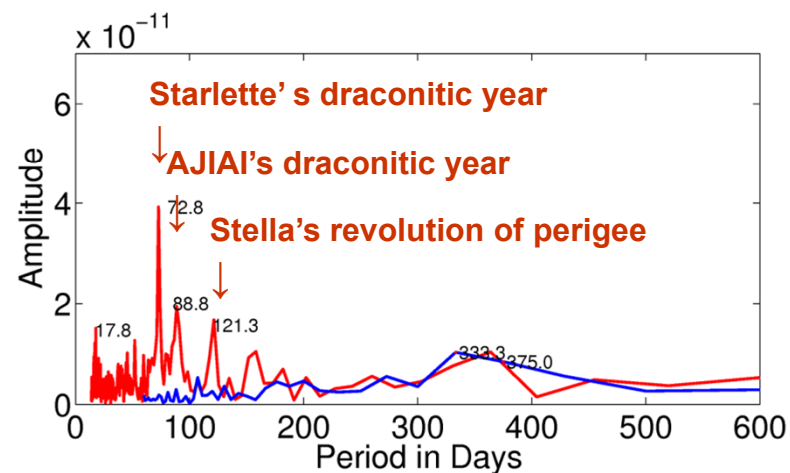
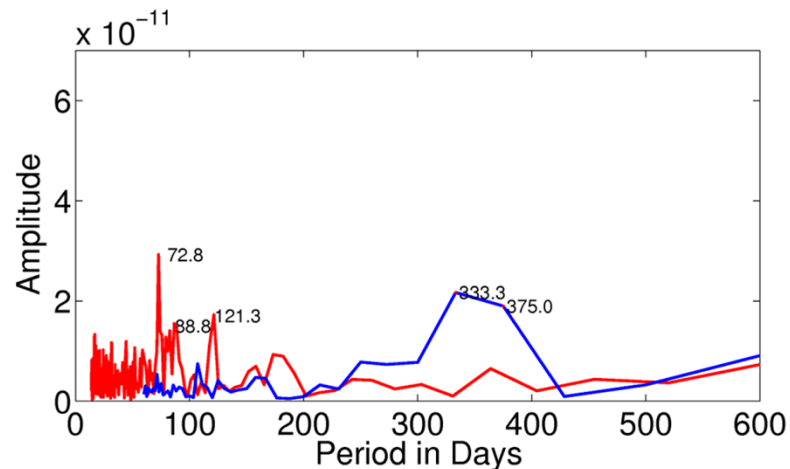
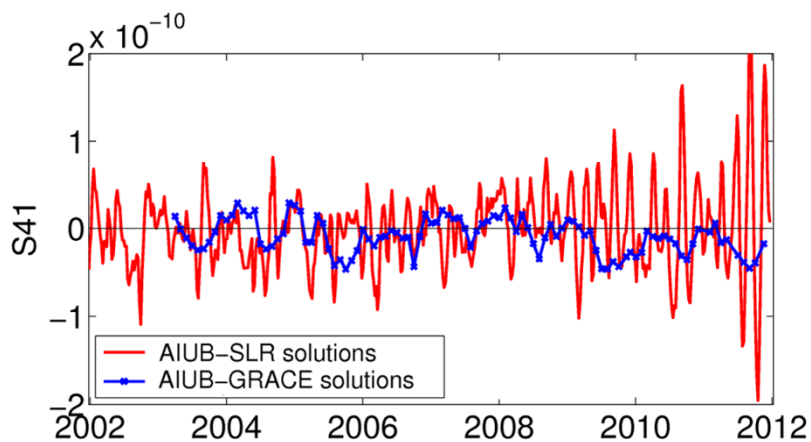
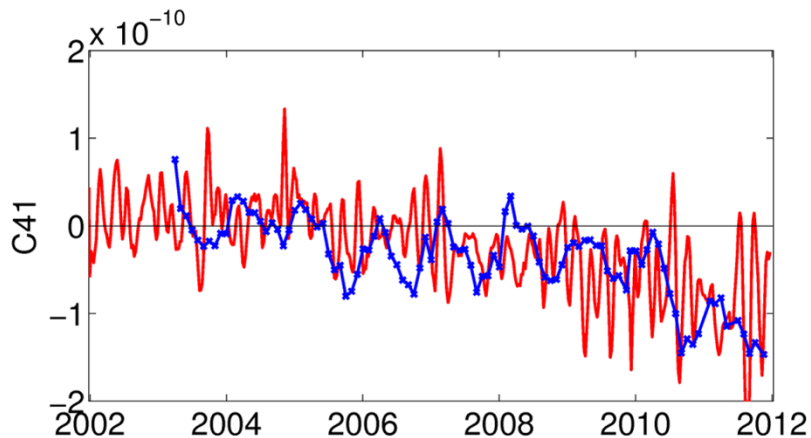
SLR vs. CHAMP vs. GRACE

Amplitudes of annual signals of low gravity field coefficients (x1e-10)



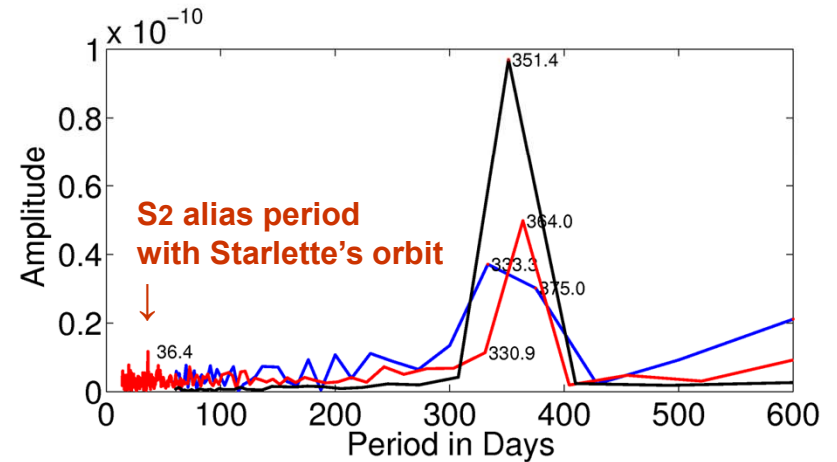
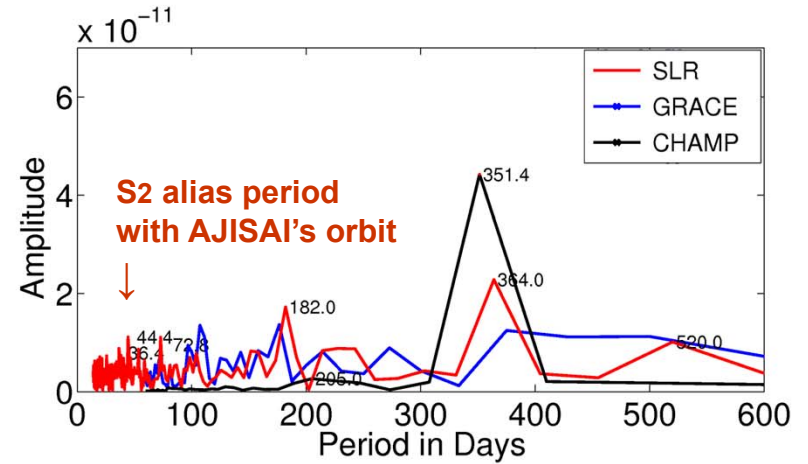
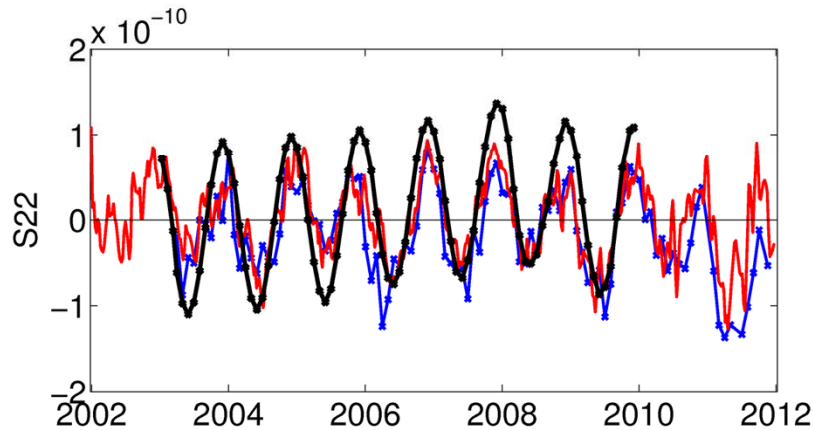
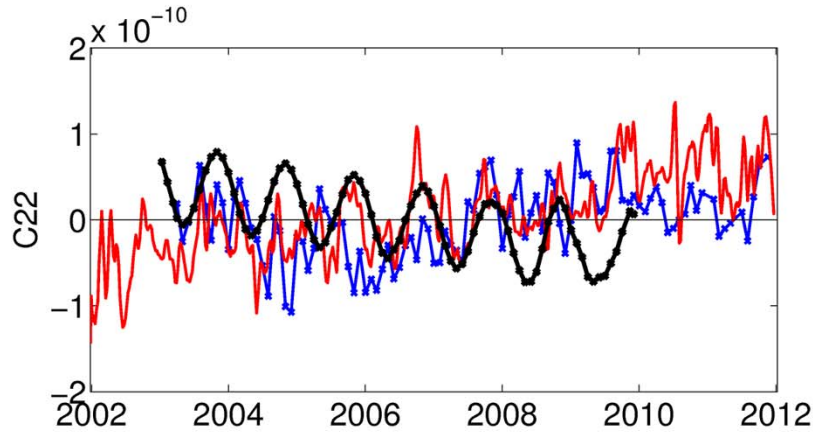
15 out of 21 (71%) coefficients up to d/o 4/4 are derived from SLR with a quality similar to GRACE's
 13 out of 21 (62%) coefficients up to d/o 4/4 are derived from CHAMP with a qual. similar to GRACE's

SLR – specific issues



C₄₁ derived by SLR shows similar secular trend to the GRACE results, but the high-frequency part is affected by correlations and modeling deficiencies

SLR – specific issues

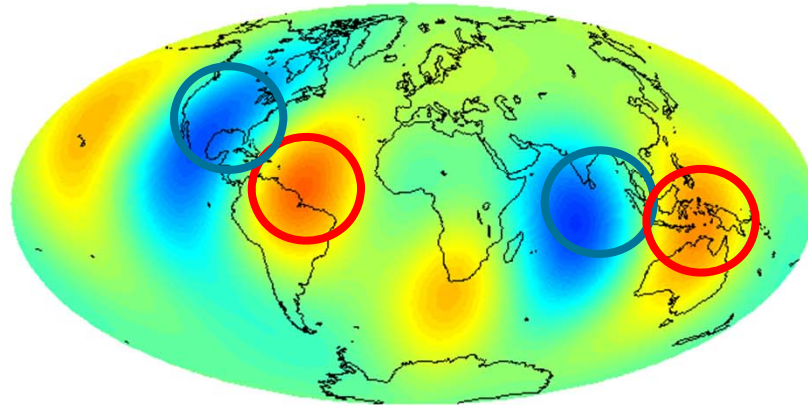


Deficiencies in S2 tide (from the background models) affect not only the GRACE solutions, but also have a minor impact on the SLR solutions.

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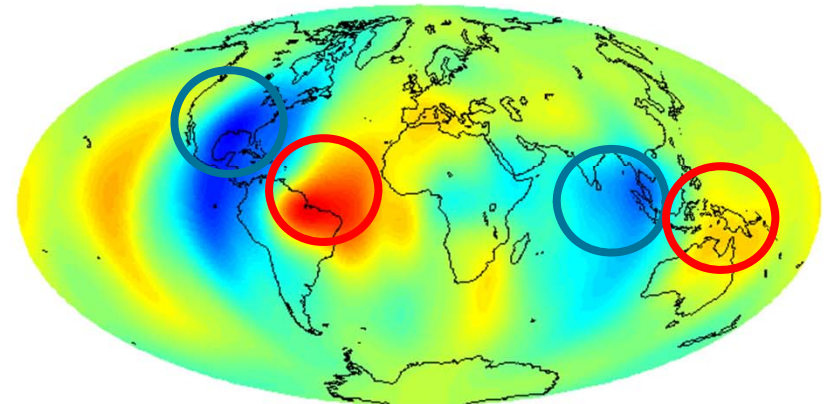
Low-degree geoid variations [mm]

AIUB-SLR, December 2004



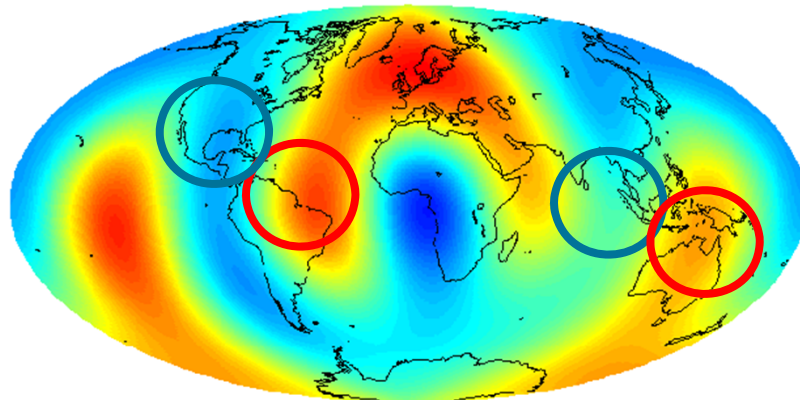
up to d/o 4/4, no filtering

AIUB-GRACE, December 2004



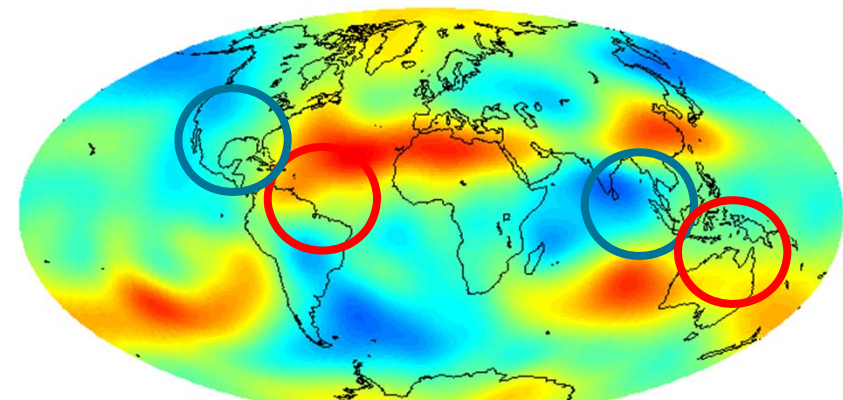
up to d/o 60/45, 1000km Gauss filter

AIUB-GNSS, December 2004

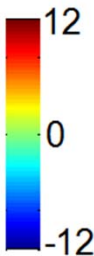


up to d/o 4/4, no filtering

AIUB-CHAMP, December 2004



up to d/o 60/60, 1000km Gauss filter



Low-degree gravity field parameters from SLR solutions fit well to the GRACE results.

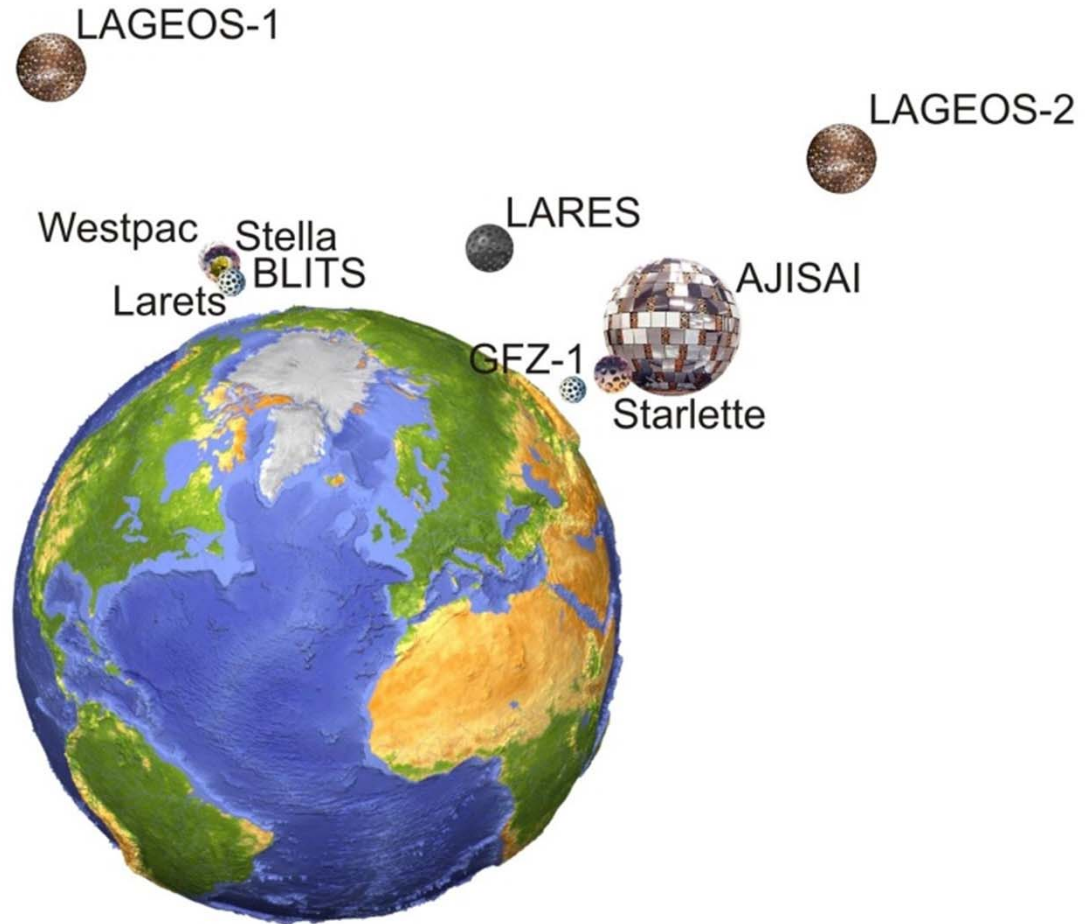
Summary

- The gravity field determination using GPS+GLONASS data is **very promising**, but **requires further investigations**.
- Most of the **low-degree** coefficients can be very **well established** by the observations of **SLR** geodetic satellites,
- Small issues related to SLR-derived gravity field coefficients originate from:
 - Deficiencies in **background models**, which are reflected, e.g., in the **S₂** alias **tide**,
 - Deficiencies in the modeling of **non-gravitational forces** (solar radiation pressure, albedo, the Yarkovsky and Yarkovsky-Schach effects),
 - **Correlations** between **gravity field parameters** (e.g., C₃₀ and C₅₀) and other parameters (e.g., **orbits**: perigee, ascending node, etc.).



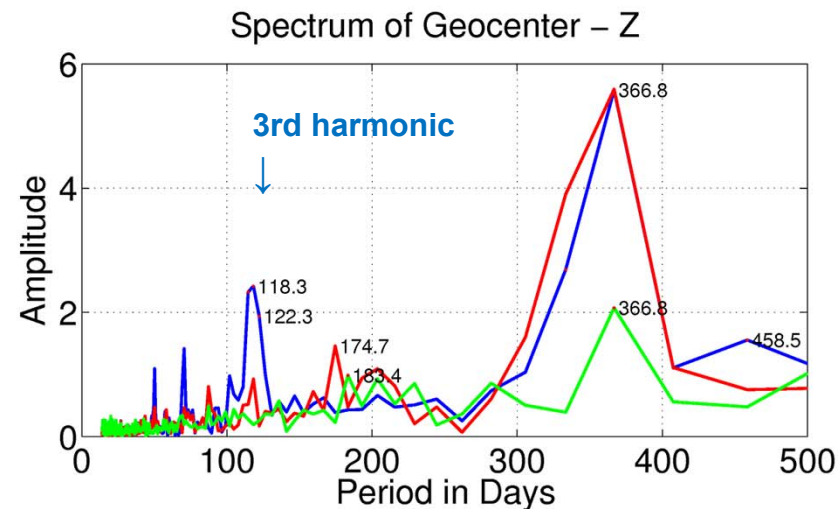
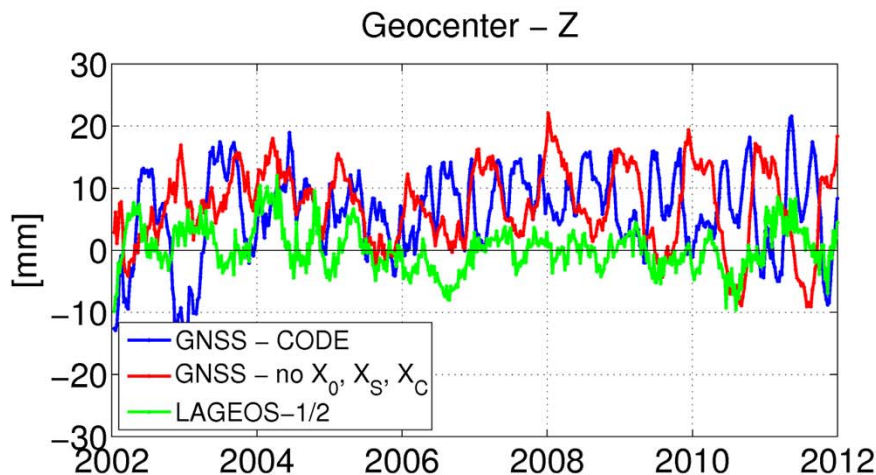
Etalon-1/2

Thank you for your attention



Geocenter coordinates from GNSS and SLR

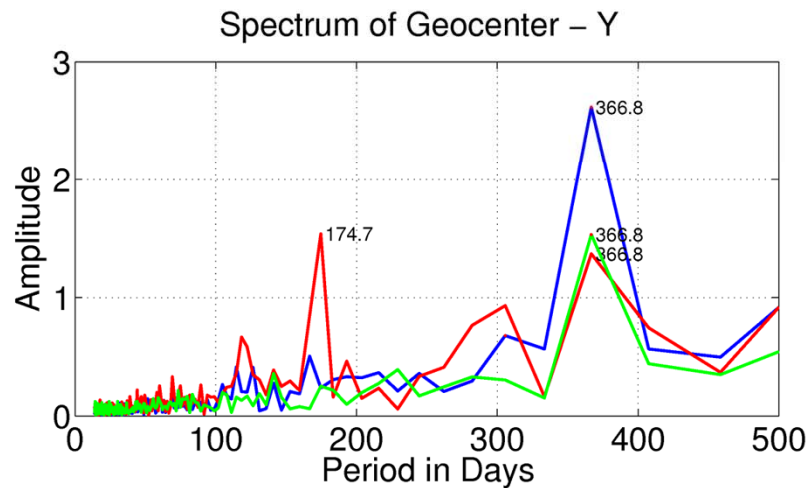
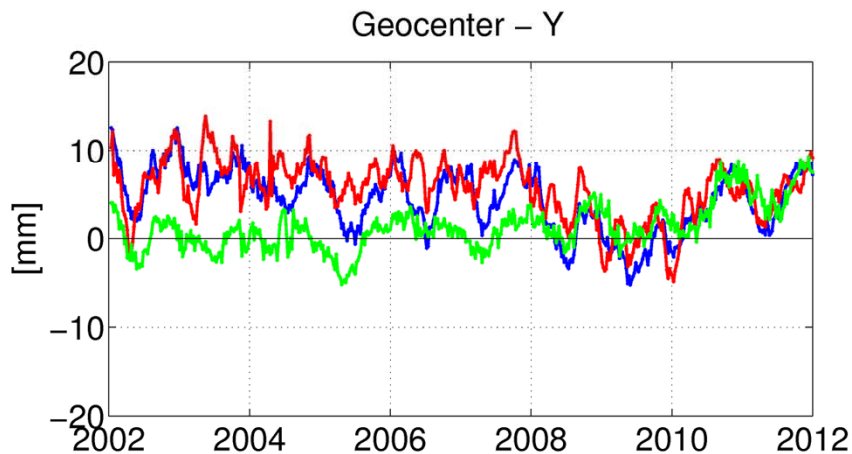
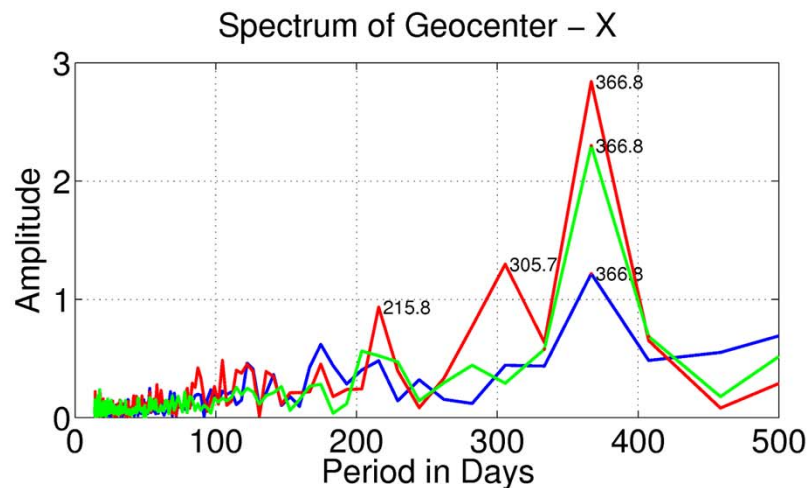
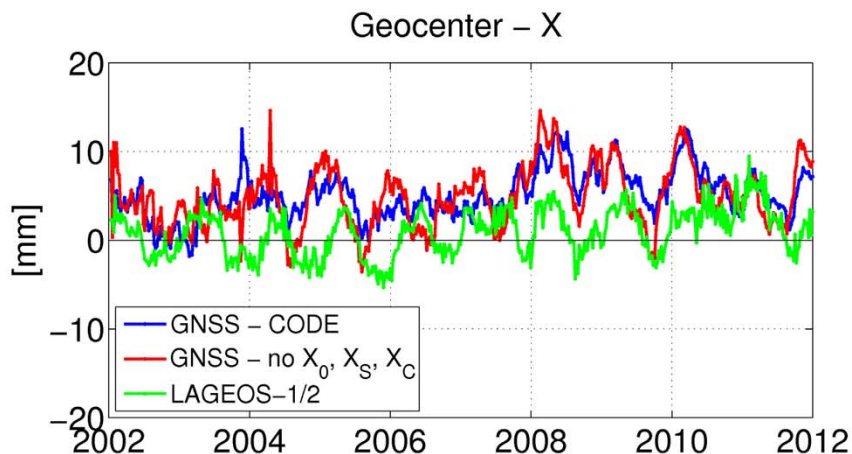
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Z geocenter component from GNSS is extremely sensitive to orbit modeling; the exclusion of dynamic orbit parameters in the X direction entirely changes the signal!

Geocenter coordinates from GNSS and SLR

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